

# Electron Transfer between Hexacyanoferrate(III) and Thiosulfate. Kinetic Studies in the *trans*-Dihydroxotetraoxosmate(VIII) Oxidation and the *trans*-Dihydroxotetraoxosmate(VIII)-catalyzed Hexacyanoferrate(III) Oxidation of Thiosulfate in Aqueous Alkaline Media

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Kinetics of oxidation of thiosulfate to tetrathionate by *trans*-dihydroxotetraoxosmate(VIII) (Os(VIII)) and by hexacyanoferrate(III) in the catalytic presence of Os(VIII) have been studied in aqueous alkaline media. The observed pseudo-first-order rate constants for disappearance of Os(VIII) in the Os(VIII)–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> system (*k*<sub>obsd</sub>), and those for disappearance of hexacyanoferrate(III) in the Os(VIII)-catalysed Fe(CN)<sub>6</sub><sup>3-</sup>–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> system (*k*<sub>cat</sub>) conform, respectively, to Eqs. A and B:

$$k_{\text{obsd}} = k_3 K_{\text{Os}} K_2 [\text{S}_2\text{O}_3^{2-}] (1 + K_{\text{Os}} [\text{OH}^-] + K_{\text{Os}} K_2 [\text{S}_2\text{O}_3^{2-}])^{-1}, \quad (\text{A})$$

$$k_{\text{cat}} = k_6 K_{\text{Os}} K_2 [\text{Os(VIII)}] [\text{OH}^-] [\text{S}_2\text{O}_3^{2-}] (1 + K_{\text{Os}} K_2 [\text{S}_2\text{O}_3^{2-}])^{-1}, \quad (\text{B})$$

where *K*<sub>Os</sub> is the stability constant of *trans*-dihydroxotetraoxosmate(VIII) in aqueous alkaline media, *K*<sub>2</sub> and *k*<sub>3</sub> are the formation and decomposition constant of the intermediate complex **1**, and *k*<sub>6</sub> refers to the rate constant of electron-transfer from **1** to hexacyanoferrate(III). The values of *K*<sub>Os</sub> and *K*<sub>2</sub>, as obtained from spectrophotometric titrations and stopped-flow spectrophotometry, respectively, are 19.5 ± 3 dm<sup>3</sup> mol<sup>-1</sup> and 5.58 ± 0.13; the computed values from kinetic data of *K*<sub>Os</sub>, *K*<sub>2</sub>, and *k*<sub>3</sub> at 30 °C and μ = 0.32 mol dm<sup>-3</sup>, and that of *k*<sub>6</sub> at 35 °C and μ = 0.32 mol dm<sup>-3</sup> are 22.5 ± 2 dm<sup>3</sup> mol<sup>-1</sup>, 6.12 ± 0.5, (3.32 ± 0.3) × 10<sup>-1</sup> dm<sup>3</sup> mol<sup>-1</sup> s<sup>-1</sup>, and (3.31 ± 0.3) × 10<sup>-2</sup> dm<sup>6</sup> mol<sup>-2</sup> s<sup>-1</sup>, respectively. Possible mechanisms for electron-transfer are discussed in terms of an initial equilibrium interaction between Os(VIII) and S<sub>2</sub>O<sub>3</sub><sup>2-</sup> forming an intermediate complex [OsO<sub>4</sub>(OH)(S<sub>2</sub>O<sub>3</sub>)<sup>3-</sup>] (**1**) followed by (a) a rate-determining decomposition of **1**, with concomitant electron-transfer, in the Os(VIII)–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> system, and (b) a rate-determining outersphere electron-transfer from **1** to hexacyanoferrate(III) in the Os(VIII)-catalyzed Fe(CN)<sub>6</sub><sup>3-</sup>–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> system.

The oxidation of thiosulfate by various metallic oxidants has been shown to proceed either through the intermediacy of metal-thiosulfato complexes<sup>1–5</sup>) formed prior to electron-transfer or without a change in the inner co-ordination sphere of the metal.<sup>6–9</sup>) We have observed<sup>7)</sup> that the oxidation of thiosulfate is zero-order in hexacyanoferrate(III) over a pH range 6.03–12.3, the main reaction being the spontaneous decomposition of thiosulfate. Similar observations were made by Howlett and Wedzicha<sup>6)</sup> who reported that the initial 5% reaction of hexacyanoferrate(III) with thiosulfate in the presence of H<sub>2</sub>(edta) and acetate was of zero-order in hexacyanoferrate(III). In the presence of 'Osmium Tetraoxide' and an 8–10% aqueous solution of potassium hydroxide, hexacyanoferrate(III) was found to oxidise thiosulfate to sulfate,<sup>10)</sup> but the details of the reaction were not presented. In the present study, we are reporting the *trans*-dihydroxotetraoxosmate(VIII)-catalyzed hexacyanoferrate(III) oxidation of thiosulfate to tetrathionate. Unlike earlier reports on the Os(VIII)-catalyzed electron-transfer reactions, the present kinetics exhibit a first-order dependence in hexacyanoferrate(III).

An understanding of the extent to which Os(VIII) can function as an electron-transfer agent is crucial to the interpretation of kinetics and mechanism of Os(VIII)-catalyzed electron-transfer reactions. Quite a few organic functions have been directly oxidized by Os(VIII); however, no study appears to have been carried out on the direct oxidation of inorganic compounds by Os(VIII). Keeping this in view, the electron-transfer in the Os(VIII)–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> system has

been studied as an extension by stopped-flow spectrophotometry.

## Experimental

**Materials and Methods.** All the chemicals used were of Analar grade, and the solutions were prepared using doubly distilled water exclusively. A requisite amount of Os(VIII) solution from the stock (prepared by dissolving 'OsO<sub>4</sub>' of Johnson-Matthey in a weakly aqueous alkaline solution, estimated by iodometry<sup>11)</sup> and stored in a cool dark place) was taken (as such for the direct oxidation by Os(VIII) or along with hexacyanoferrate(III) solution in the case of catalyzed reactions), made up, thermostated and mixed with the thiosulfate solution at appropriate pH and ionic strength. The ionic strength (μ) of the medium was adjusted by the addition of a required amount of the supporting electrolyte, sodium sulfate. The pH of the medium (±0.01), maintained by the addition of suitable amounts of standard aqueous buffers or carbonate-free hydroxide, as the case may be, was recorded by a Systronics 335 digital pH meter both before and after the reaction; the hydroxide concentrations were calculated from the mean recorded pH after correcting for the ionic strength effect of the medium. The Os(VIII)-catalyzed hexacyanoferrate(III) oxidation reactions were performed by mixing 1 ml aliquots of reactant solutions in a 1 cm-quartz cell by means of semimicro syringes. The course of the reactions was monitored for the decrease in absorbance of hexacyanoferrate(III), continuously as a function of time, at 420 nm ( $\epsilon_{420}$  9.8 × 10<sup>3</sup> dm<sup>3</sup> mol<sup>-1</sup> cm<sup>-1</sup>), in a Pye Unicam SP 1800 spectrophotometer maintained at a desired temperature (±0.1 °C). An extended absorbance scale was used for experiments in which lower concentration of the oxidant was taken.

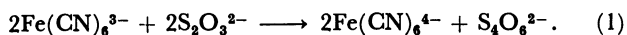
The electronic spectrum of an aqueous alkaline solution of *trans*-OsO<sub>4</sub>(OH)<sub>2</sub><sup>2-</sup>, abbreviated as Os(VIII), showed characteristic bands at 316 nm ( $\epsilon_{316}$  500 dm<sup>3</sup> mol<sup>-1</sup> cm<sup>-1</sup>) and 247 nm ( $\epsilon_{247}$  690 dm<sup>3</sup> mol<sup>-1</sup> cm<sup>-1</sup>); earlier workers<sup>11</sup>) did not report this observation. In visible region, the solution absorbed strongly around 390 nm, the absorption decreasing with increasing wavelength but without any characteristic maximum in the 390–750 nm region. Tetrathionate, the oxidation product of thiosulfate, absorbed significantly around 247 nm. The kinetic runs for the Os(VIII)–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> system were, therefore, followed by monitoring the disappearance of OsO<sub>4</sub>(OH)<sub>2</sub><sup>2-</sup> at 316 nm in an Aminco stopped-flow spectrophotometer with quartz windows and a 1 cm-light path coupled to a Beckman D. U. monochromator. The nominal mixing time for this spectrophotometer is 0.2 ms. For every entry, at least five replicate runs were performed.

The pseudo-first-order rate constants were computed by least-squares analysis of the expression:  $-\ln[(A_t - A_\infty)/(A_0 - A_\infty)] = k_{\text{obsd}}t$ , where  $A_t$ ,  $A_0$ , and  $A_\infty$ , respectively, represent the absorbance of the reactant at time 't', the initial absorbance and the absorbance at effective infinite time.

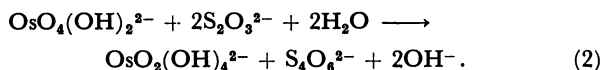
For experiments where [Substrate]<sub>0</sub> > [Oxidant]<sub>0</sub>, the second-order rate constants ( $k'$ ) were calculated by the usual method; for these experiments the first-order rate constants were calculated from the expression: First-order-rate constant =  $k'[\text{Substrate}]_0$ .

Computations were done by a D. C. M. Data Products minicomputer Microsystem 1121. The self-decomposition of thiosulfate in air was found to be negligible in the conditions employed.

**Stoichiometry.** The stoichiometric experiments were performed in the presence of  $7.8 \times 10^{-7}$  mol dm<sup>-3</sup> of Os(VIII) and in the absence of sodium sulfate. The experiments for the stoichiometric runs were carried out at 35 °C under the conditions of  $[\text{S}_2\text{O}_3^{2-}]_0 \geq [\text{Fe}(\text{CN})_6^{3-}]_0$ ; for higher concentrations of hexacyanoferrate(III), under the conditions of  $[\text{S}_2\text{O}_3^{2-}]_0 \geq [\text{Fe}(\text{CN})_6^{3-}]_0$ , the runs were carried out at 35 °C and at pH 11.3 till the reaction, with respect to hexacyanoferrate(III), was complete (Table 1). The unconsumed  $[\text{S}_2\text{O}_3^{2-}]_\infty$  was determined iodimetrically. Tests for tetrathionate were done following an earlier procedure.<sup>12</sup>) The observed stoichiometric ratio ( $\Delta[\text{Fe}(\text{CN})_6^{3-}]/\Delta[\text{S}_2\text{O}_3^{2-}]$ ) of  $0.98 \pm 0.02$  is in accord with the overall Eq. 1:



In the oxidation of thiosulfate in aqueous medium at pH 11.3 and 35 °C, 1 mol of Os(VIII) consumed  $1.96 \pm 0.03$  mol of thiosulfate (Table 1) conforming to the formation of tetrathionate.



On allowing the final reaction solution to stand for 24 h at room temperature ( $\approx 35$  °C), it was observed that about 80% of the originally consumed thiosulfate was being reformed. Back-formation of thiosulfate in reaction mixtures of completed thiosulfate oxidation has been reported earlier and explained<sup>13</sup>) to be due to the hydrolysis of tetrathionate. The reformation is, however, very slow and does not complicate the kinetics studied.

## Results and Discussion

### Electron-transfer in the Os(VIII)–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> System.

In weakly alkaline solutions, OsO<sub>4</sub> appears to exist

TABLE 1. STOICHIOMETRIC DATA<sup>a)</sup> FOR THE OXIDATION OF S<sub>2</sub>O<sub>3</sub><sup>2-</sup> (AQUEOUS MEDIUM, pH 11.3, 35 °C) Fe(CN)<sub>6</sub><sup>3-</sup>–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> system (Os(VIII)<sup>b)</sup>-catalyzed)

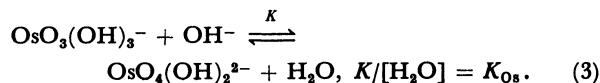
$10^3 [\text{Fe}(\text{CN})_6^{3-}]_0^c$	$10^3 [\text{S}_2\text{O}_3^{2-}]_0$	$10^3 [\text{S}_2\text{O}_3^{2-}]_\infty^d$
0.01	0.1	— <sup>f)</sup>
0.01	0.05	0.039 <sup>f, g)</sup>
0.1	0.2	0.1 <sup>g)</sup>
0.2	1.0	0.79 <sup>g)</sup>
0.4	0.5	0.098 <sup>g)</sup>
0.5	1.0	0.49 <sup>g)</sup>
5.0	10.0	4.95 <sup>g)</sup>
5.0	10.02	8.1 <sup>h)</sup>
5.0	10.0	9.1 <sup>i)</sup>
5.01	5.95	4.9 <sup>i)</sup>

Os(VIII)–S <sub>2</sub> O <sub>3</sub> <sup>2-</sup> system			
$10^3 [\text{Os(VIII)}]_0^e$	$10^3 [\text{S}_2\text{O}_3^{2-}]_0$	$10^3 [\text{Os(VIII)}]_\infty^e$	$10^3 [\text{S}_2\text{O}_3^{2-}]_\infty^d$
2.0	1.0	1.48	
2.5	1.1	1.94	
3.2	1.2	2.58	
4.1	1.0	3.58	
5.0	1.0	4.49	
0.93	2.1		0.3 <sup>g)</sup>
0.94	3.0		1.2 <sup>g)</sup>
0.92	4.0		2.2 <sup>g)</sup>
0.98	5.2		4.3 <sup>g)</sup>
5.0	16.7		14.8 <sup>h)</sup>
10.1	22.0		18.0 <sup>i)</sup>

a) All concentration units are in mol dm<sup>-3</sup>. b) In the presence of  $7.8 \times 10^{-7}$  mol dm<sup>-3</sup> of Os(VIII). c) Key: o; initial concentration,  $\infty$ ; final concentration when the reaction is effectively over. d) Analysis by iodimetry in the presence of zinc sulfate solution just after the reaction is effectively complete. e) Analysis by spectrophotometry at 316 nm. f) At 45 °C. g) Analysis just after the reaction is complete. h) Analysis after keeping the final reaction solution at 35 °C for 24 h. i) Analysis after keeping the final reaction at 60 °C for 5 h (after h).

in the form of OsO<sub>3</sub>(OH)<sub>3</sub><sup>-</sup> which combines with OH<sup>-</sup> to yield the reactive form of Os(VIII), *trans*-OsO<sub>4</sub>(OH)<sub>2</sub><sup>2-</sup>. This is in accord with the findings of Sauerbrum and Sandell<sup>13</sup>) on the dissociation of osmic acid.



( $K_{\text{Os}} = 24 \pm 4$  dm<sup>3</sup> mol<sup>-1</sup> at 25 °C and  $\mu = 1.0$  mol dm<sup>-3</sup>,  $\Delta H$  and  $\Delta S$  associated with this equilibrium are  $24 \pm 1$  kJ mol<sup>-1</sup> and  $-146 \pm 6$  J K<sup>-1</sup> mol<sup>-1</sup>).<sup>11</sup>)

Applying Benesi-Hildebrand equation<sup>14</sup>) for the determination of equilibrium constant and  $\epsilon$ ,

$$[\text{Os(VIII)}]_0 A^{-1} = (K\epsilon[\text{OH}^-])^{-1} + \epsilon^{-1} \text{ at } [\text{Os(VIII)}]_0 < [\text{OH}^-], \quad (4)$$

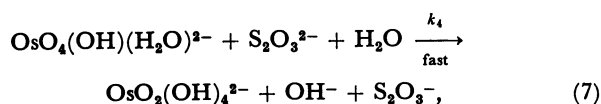
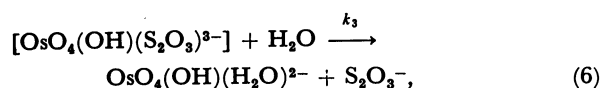
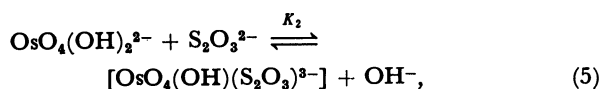
where  $[\text{Os(VIII)}]_0$  is the total analytical concentration

of Os(VIII) fixed by iodometry, and  $A$  and  $\epsilon$  respectively refer to the absorbance and molar absorptivity of the complex at 316 nm, the values of  $K_{Os}$  and  $\epsilon_{316}$  at 30 °C and  $\mu=0.32$  mol dm<sup>-3</sup> have been obtained by a weighted non-linear least-squares programme of the absorbance data at various  $[Os(VIII)]_0$  and  $[OH^-]$  ( $[Os(VIII)]_0$   $0.6 \times 10^{-4}$ – $20.4 \times 10^{-4}$  mol dm<sup>-3</sup>,  $[OH^-]$   $1 \times 10^{-3}$ – $40.1 \times 10^{-3}$  mol dm<sup>-3</sup>) as  $19.5 \pm 3$  dm<sup>3</sup> mol<sup>-1</sup> and  $500 \pm 20$  dm<sup>3</sup> mol<sup>-1</sup> cm<sup>-1</sup>, respectively; these values should be independent of the concentrations of Os(VIII) and OH<sup>-</sup> employed. The  $K_{Os}$  value of this work is in good agreement with that obtained earlier.<sup>11)</sup>

The Os(VIII)–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> reaction exhibits a first-order dependence on  $[Os(VIII)]$  in the range  $0.45 \times 10^{-4}$ – $9.06 \times 10^{-4}$  mol dm<sup>-3</sup>. At 316 nm, first there is an abrupt increase in the absorbance ( $t_{1/2} \approx 125$  ms) followed by a subsequent slower step where the absorbance decreases. The first step probably represents a fast formation of an intermediate complex and is followed by a slower decay. The  $k_{obsd}$  value (corresponding to the decrease in absorbance) at a constant  $[S_2O_3^{2-}]_0$  ( $=5.0 \times 10^{-2}$  mol dm<sup>-3</sup>) registers a marginal increase with the increase in  $[OH^-]$  from  $6.18 \times 10^{-3}$  mol dm<sup>-3</sup> to  $1.0 \times 10^{-2}$  mol dm<sup>-3</sup>, remains almost unchanged till  $[OH^-]=3.06 \times 10^{-2}$  mol dm<sup>-3</sup>, and decreases significantly at much higher  $[OH^-]$ . The  $k_{obsd}$  is found to increase almost linearly with increasing  $[S_2O_3^{2-}]$  for  $[S_2O_3^{2-}]_0=1.0 \times 10^{-4}$ – $10 \times 10^{-3}$  mol dm<sup>-3</sup>; however, beyond  $[S_2O_3^{2-}]$  of  $50 \times 10^{-3}$  mol dm<sup>-3</sup>, the  $k_{obsd}$  varies only slightly by about 5% for an almost two-fold increase in  $[S_2O_3^{2-}]$ . The rate expression for the reduction of Os(VIII) should, therefore, include a distinct  $[S_2O_3^{2-}]$ -dependent term, getting saturated at higher  $[S_2O_3^{2-}]$ .

The  $k_{obsd}$  increases with an increase in ionic strength of the medium. It does not appreciably change in the range 25–45 °C. Added acrylonitrile retards the rate, but no polymerisation could be observed.

**Rate Law and Mechanism:** The preliminary kinetic results suggest that the mechanism of reduction of Os(VIII) by S<sub>2</sub>O<sub>3</sub><sup>2-</sup> involves incorporation of a thiosulfato-ligand into the inner-coordination sphere of Os(VIII) prior to an electron-transfer step.



Since S<sub>2</sub>O<sub>3</sub><sup>2-</sup> is an effective one-electron reducing agent, an Os(VII) species will probably be produced which will further get reduced rapidly to Os(VI) with another S<sub>2</sub>O<sub>3</sub><sup>2-</sup>. Os(VII) is known in solution<sup>16)</sup> and has been prepared in solid state.<sup>17)</sup> Such a one-electron change can take place only with a high activation enthalpy because two very unstable species

are formed (Eq. 6) and that the subsequent step, Os(VII) + e<sup>-</sup> → Os(VI), can proceed without obstacle.

Consequently, the mechanism of the reaction would result in the rate law (Eq. 9), on the basis of Eqs. 3, 5–8, and on applying a steady-state treatment to the intermediate complex  $[OsO_4(OH)(S_2O_3)^{2-}]$  (1)

$$-\frac{d[Os(VIII)]}{dt} = \frac{k_3 K_{Os} K_2 [Os(VIII)]_T [S_2O_3^{2-}]}{1 + K_{Os} [OH^-] + K_{Os} K_2 [S_2O_3^{2-}]}, \quad (9)$$

where the total analytical  $[Os(VIII)]_T = [OsO_3(OH)_3^-] + [OsO_4(OH)_2^{2-}] + [OsO_4(OH)(S_2O_3)^{2-}]$ . If as a first approximation, a reasonable assumption is made that at the low  $[OH^-]$  employed,  $K_{Os} [OH^-] \ll (1 + K_{Os} \times K_2 [S_2O_3^{2-}])$ , Eq. 10 is obtained.

$$-\frac{d[Os(VIII)]}{dt} = \frac{k_3 K_{Os} K_2 [Os(VIII)]_T [S_2O_3^{2-}]}{1 + K_{Os} K_2 [S_2O_3^{2-}]}, \quad (10)$$

$$k_{obsd} = k_3 K_{Os} K_2 [S_2O_3^{2-}] (1 + K_{Os} K_2 [S_2O_3^{2-}])^{-1}, \quad (11)$$

which on rearrangement becomes

$$(k_{obsd})^{-1} = (k_3)^{-1} + (k_3 K_{Os} K_2)^{-1} ([S_2O_3^{2-}])^{-1}. \quad (12)$$

Eq. 12 predicts that  $(k_{obsd})^{-1}$  should be a linear function of  $([S_2O_3^{2-}])^{-1}$ . From the intercept and slope of this least-squares plot (Fig. 1), using the experimentally determined  $K_{Os}$  value, the  $k_3$  and  $K_2$  values have been computed respectively as  $(3.32 \pm 0.3) \times 10^{-1}$  dm<sup>3</sup> mol<sup>-1</sup> s<sup>-1</sup> and  $6.12 \pm 0.5$  at 30 °C and 0.32 mol dm<sup>-3</sup> of ionic strength. The computed  $K_2$  is very close to the average value (5.58) of the observed constant pertaining to the first abrupt increase in the absorbance at 316 nm. Also the agreement of the  $k_{calcd}$  (Eq. 12) values obtained (employing the estimated values of  $k_3$ ,  $K_2$ , and the experimental value of  $K_{Os}$ ) with the experimentally determined  $k_{obsd}$  is in support of the postulated mechanism.

Eq. 9 can be rearranged to Eq. 13:

$$(k_{obsd})^{-1} = (1 + K_2 [S_2O_3^{2-}] K_{Os}) (k_3 K_2 [S_2O_3^{2-}] K_{Os})^{-1} + [OH^-] (k_3 K_2 [S_2O_3^{2-}])^{-1}. \quad (13)$$

At  $[S_2O_3^{2-}]_0 = 5.0 \times 10^{-2}$  mol dm<sup>-3</sup>, employing the value of  $k_3$  computed earlier,  $K_{Os}$  has been calculated from the least-squares slope and intercept of the  $(k_{obsd})^{-1}$  vs.  $[OH^-]$  plot as  $22.5 \pm 2$  at 30 °C and  $\mu = 0.32$  mol dm<sup>-3</sup>. This value is quite close to that experimentally determined. There is also agreement of the  $k_{calcd}$  (Eq. 13) values with the  $k_{obsd}$  values (Table 2).

Supporting evidences from kinetics or otherwise,

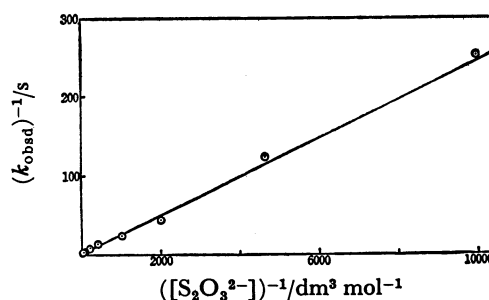


Fig. 1.  $1/k_{obsd}$  vs.  $1/[S_2O_3^{2-}]$  (The Os(VIII)–S<sub>2</sub>O<sub>3</sub><sup>2-</sup> reaction)  $[Os(VIII)] = 6 \times 10^{-4}$ ,  $[OH^-] = 1 \times 10^{-2}$ ; Aqueous medium, 30 °C,  $\mu = 0.32$  (All concentrations are in mol dm<sup>-3</sup>).

TABLE 2. TYPICAL AVERAGE<sup>a)</sup> RATE CONSTANTS FOR THE REACTION BETWEEN Os(VIII) AND S<sub>2</sub>O<sub>3</sub><sup>2-</sup> (Aqueous medium, 30 °C,  $\mu=0.32^b$ )

10 <sup>4</sup> [Os(VIII)] <sub>0</sub>	10 <sup>3</sup> [S <sub>2</sub> O <sub>3</sub> <sup>2-</sup> ] <sub>0</sub>	10 <sup>2</sup> [OH <sup>-</sup> ]	$k_{\text{obsd}}/\text{s}^{-1}$ c)	$k_{\text{calcd}}/\text{s}^{-1}$
9.00	52	1.10	0.42 <sup>d)</sup>	
9.00	50	1.10	0.50 <sup>e)</sup>	
9.01	51	(6.18 × 10 <sup>-8</sup> ) <sup>m)</sup>	0.23	0.29 <sup>l)</sup>
9.04	110	(6.18 × 10 <sup>-8</sup> ) <sup>m)</sup>	0.24	0.29 <sup>l)</sup>
9.02	50	(4.28 × 10 <sup>-6</sup> ) <sup>m)</sup>	0.24	0.29 <sup>l)</sup>
9.06	51	1.00	0.33	0.282 <sup>l)</sup>
9.03	50	2.12	0.32	0.274 <sup>l)</sup>
9.05	51	3.06	0.315	0.27 <sup>l)</sup>
9.13	50	50.6	0.12	0.12 <sup>l)</sup>
9.10	50	110	0.07	0.07 <sup>l)</sup>
9.00	51	1.10	0.32 <sup>f)</sup>	
9.06	51	1.00	0.33 <sup>g)</sup>	
9.03	51	1.08	0.33 <sup>h)</sup>	
3.00	53	1.03	0.32	
3.10	53	1.30	0.33 <sup>i)</sup>	
3.05	50.5	1.20	0.32 <sup>i)</sup>	
1.70	49	1.15	0.33	
9.04	51	1.02	0.19 <sup>j)</sup>	
1.51	5.01	1.03	5.52*	
3.01	5.01	1.02	5.57*	
5.06	5.02	1.00	5.53*	
6.00	5.03	1.00	5.74*	
6.05	5.0	1.05	5.01* <sup>f)</sup>	
6.05	5.01	1.06	5.38* <sup>g)</sup>	
6.03	5.01	1.01	6.48* <sup>h,k)</sup>	
9.03	5.0	1.07	5.71*	
3.02	7.0	1.04	5.50*	
3.02	10.1	1.03	5.46*	
3.02	50.1	1.05	5.61*	

a) Standard deviations range from  $\pm 0.02$  to  $0.1$  (at least five experiments for each entry). b) All concentration units in mol dm<sup>-3</sup>. c) Average first-order rate constants with respect to the disappearance of Os(VIII) at 316 nm. d,e) Respectively at 0.42 and 0.52 mol dm<sup>-3</sup> of ionic strength. f,g,h) Respectively at 25, 40, and 45 °C. i) For the appearance of OsO<sub>4</sub>(OH)<sub>2</sub><sup>2-</sup> at 500 nm ( $\Delta A/\Delta t > 0$ ). j) In the presence of  $1 \times 10^{-4}$  mol dm<sup>-3</sup> of acrylonitrile. k) Average  $\Delta H^*$  and  $\Delta S^*$  respectively 7.1 kJ mol<sup>-1</sup> and  $-207 \text{ J K}^{-1} \text{ mol}^{-1}$ . l) Average  $k_{\text{calcd}}$  from Eq. 13 (representative). m) Calculated from measured pH. \* Calculated for the first abrupt increase in absorbance of Os(VIII) at 316 nm.

have been well presented for the formation of intermediate complexes between metal ions and thiosulfate.<sup>1-5)</sup> In the Os(VIII)-S<sub>2</sub>O<sub>3</sub><sup>2-</sup> system also, the kinetic evidences and the abrupt increase in absorbance at 316 nm, as soon as Os(VIII) and thiosulfate are mixed, are suggestive of the inner-sphere substitution of a hydroxo-ligand by a thiosulfato-ligand in the *trans*-OsO<sub>4</sub>(OH)<sub>2</sub><sup>2-</sup>.

The attack by the sulfur-end rather than by the oxygen-end of thiosulfate is consistent<sup>18,4)</sup> with the value of the formation constant of the intermediate complex [OsO<sub>4</sub>(OH)(S<sub>2</sub>O<sub>3</sub>)<sup>3-</sup>]. Spectrophotometric titrations could not be performed because of the ra-

pidity of the change in absorbance of Os(VIII) and also due to the considerable absorption of tetrathionate between 240–290 nm. However, we got indications for the formation of a 1:1 intermediate complex involving Os(VIII) and thiosulfate by the following method. Zero-time absorbance at 316 nm were obtained by extrapolation for different [Os(VIII)]: [S<sub>2</sub>O<sub>3</sub><sup>2-</sup>] ratios in isomolar and non-isomolar mixtures. When the increase in the absorbance difference,  $+\Delta A$ , was plotted against the mole-fraction of Os(VIII), a maximum in  $\Delta A$  was observed at the mole-fraction of Os(VIII)=0.5.

It is more rational to assume that an electron-transfer from thiosulfate to Os(VIII) has taken place during the substitution. The activated complex could then offer, at the same time, the lowest energy barrier to substitution and also to electron-transfer (Eq. 5), since the orbitals of the central osmium are disturbed (Table 2, foot note for activation parameters pertaining to the first abrupt increase in absorbance at 316 nm); the process starts as a substitution and continues with a one-electron transfer. Since *trans*-dihydroxotetraoxosmate(VIII) ends up finally as *trans*-dioxotetrahydroxosmate(VI), an equatorial attack by the outer-sulfur of thiosulfate on osmium is likely,<sup>15b)</sup> leading to a fair degree of displacement of the axial hydroxo-ligand.

*Os(VIII)-catalyzed Fe(CN)<sub>6</sub><sup>3-</sup>-S<sub>2</sub>O<sub>3</sub><sup>2-</sup> Electron-transfer.* Studies on Os(VIII)-catalysed oxidation reactions of various inorganic<sup>11)</sup> and organic substrates<sup>19)</sup> by hexacyanoferrate(III) are increasingly becoming useful probes in the elucidation of the nature of oscillatory catalysis of Os(VIII). In these studies and in numerous other studies of Os(VIII)-catalyzed oxidations by other oxidants,<sup>20,21)</sup> Os(VIII) is involved in an initial equilibrium formation of an intermediate Os(VIII)-substrate complex which breaks down rate-determiningly to the products and Os(VI); the Os(VI) formed is oxidised rapidly to Os(VIII) by the main oxidant, resulting in zero-order kinetics with respect to the main oxidant.

In contrast to the earlier observations, the Os(VIII)-catalysed hexacyanoferrate(III) oxidation of thiosulfate is first-order in hexacyanoferrate(III) over the [Fe(CN)<sub>6</sub><sup>3-</sup>]<sub>0</sub> range  $0.1 \times 10^{-4}$ – $20.1 \times 10^{-4}$  mol dm<sup>-3</sup>. The observation is interesting as it is probably the first report of a main oxidant exhibiting first-order kinetics in the presence of an oscillatory catalyst.

At constant ionic strength and constant [Na<sup>+</sup>] ([Na<sup>+</sup>]  $\gg$  [K<sup>+</sup>]), the  $k_{\text{cat}}$  value linearly increases with the increase in [S<sub>2</sub>O<sub>3</sub><sup>2-</sup>], [Os(VIII)], or [OH<sup>-</sup>] for their respective ranges of concentration:  $1.0 \times 10^{-5}$ – $2.46 \times 10^{-3}$ ,  $3.9 \times 10^{-7}$ – $97.3 \times 10^{-7}$ , and  $1.0 \times 10^{-5}$ – $50.5 \times 10^{-3}$  mol dm<sup>-3</sup> (Fig. 2). Also the good reproducibility of the  $k_{\text{cat}}$  value obtained by following the first-order disappearance of thiosulfate at 217 nm (in a representative run) with that obtained by monitoring the disappearance of hexacyanoferrate(III), shows that the rate of disappearance of thiosulfate is the same as that of hexacyanoferrate(III). There is a retardation in the rate in the presence of added mannitol, acrylonitrile or hexacyanoferrate(II) in this system (Table 3).

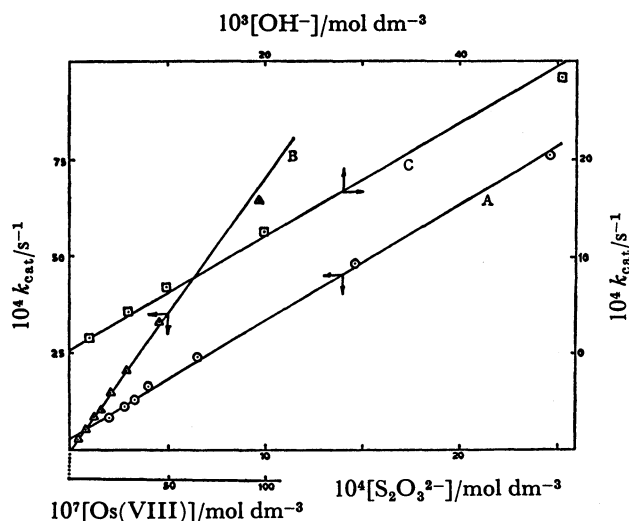
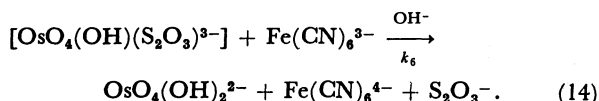


Fig. 2.  $k_{cat}$  vs.  $[S_2O_3^{2-}]$ ,  $[OH^-]$  or  $[Os(VIII)]$  (The Os(VIII)-catalyzed  $Fe(CN)_6^{3-}$ - $S_2O_3^{2-}$  reaction).

A:  $[OH^-] = 1 \times 10^{-2}$ ,  $[Os(VIII)] = 7.8 \times 10^{-7}$ ; B:  $[S_2O_3^{2-}] = 1.2 \times 10^{-4}$ ,  $[OH^-] = 1 \times 10^{-2}$ ; C:  $[S_2O_3^{2-}] = 1.6 \times 10^{-4}$ ,  $[Os(VIII)] = 7.8 \times 10^{-7}$ ;  $[Fe(CN)_6^{3-}] = 1 \times 10^{-4}$ , aqueous medium,  $35^\circ C$ ,  $\mu = 0.32$  (All concentrations are in  $mol\ dm^{-3}$ ).

The  $k_{cat}$  value increases linearly with  $\mu$ . Considerable ion-pairing has been reported in oxidations by alkaline hexacyanoferrate(III), but in the present case as the rate is independent of the  $[Fe(CN)_6^{3-}]_0$ , any ion-pairing between  $K^+$  or  $Na^+$  and hexacyanoferrate(III) will have no significant effect<sup>22)</sup> on the rate. A plot of oxidation rate ( $k_{cat}$ ) against  $\mu$  yields a straight line with no zero-rate at zero-electrolyte concentration. This, therefore, appears to be a mere ionic strength effect.<sup>15a)</sup> A plot of  $\log k_{cat}$  vs.  $\mu^{1/2}$  is also linear, but no meaningful inference regarding the charge of the reacting ions could be drawn<sup>23a)</sup> from the slope of the straight line, as the oxidation process is a multi-step one.

**Rate Law and Mechanism:** In the absence of Os(VIII), the oxidation of thiosulfate by hexacyanoferrate(III) does not virtually proceed<sup>7)</sup> under the conditions employed for the catalysed oxidation, demonstrating that the presence of catalytic amounts of Os(VIII) accelerates the reaction tremendously. The observed kinetic data for the catalyzed system can be presented in terms of a reaction scheme consisting of Eqs. 3, 5, and 14.



Since in the catalysed system,  $[S_2O_3^{2-}] \gg [Os(VIII)] \ll [Fe(CN)_6^{3-}]$ , the contribution of the catalytic  $[Os(VIII)]$  to the direct oxidation of thiosulfate is negligible. Applying steady-state treatment to  $[OsO_4(OH)(S_2O_3^{3-})]$ , a rate expression can be derived as in Eq. 15.

$$-\frac{d[Fe(CN)_6^{3-}]}{dt} = \frac{k_6 K_{Os} K_2 [Os(VIII)] [Fe(CN)_6^{3-}] [OH^-] [S_2O_3^{2-}]}{1 + K_{Os} K_2 [S_2O_3^{2-}]}, \quad (15)$$

TABLE 3. TYPICAL AVERAGE<sup>a)</sup> RATE CONSTANTS FOR Os(VIII)-CATALYZED  $Fe(CN)_6^{3-}$  OXIDATION OF  $S_2O_3^{2-}$  (Aqueous medium,  $35^\circ C$ ,  $\mu = 0.32$ ,<sup>b)</sup>  $[Fe(CN)_6^{3-}]_0 = (1.0-1.05) \times 10^{-4}$ ,  $[Os(VIII)] = 7.8 \times 10^{-7}$ ,  $[OH^-] = (10.0-10.2) \times 10^{-3}$ )

$10^4 [S_2O_3^{2-}]_0$	$10^4 k_{cat}/s^{-1}$ c)	$10^4 k_{cat}(calcd)/s^{-1}$ d)
1.23	5.00	4.79
1.25	5.17	4.87
1.61	6.70	6.24
2.00	7.78	7.72
2.17	8.84	8.36
2.80	11.15	10.70
3.28	13.20	12.50
4.00	16.40	15.10
6.45	24.00	23.70
14.6	48.0	49.1
24.6	76.0	75.2
2.10	7.53 <sup>e)</sup>	
0.1	0.4 <sup>f)</sup>	0.40
1.25	5.20 <sup>e)</sup>	4.87
2.80	12.20 <sup>g)</sup>	
2.80	17.74 <sup>h)</sup>	
2.81	11.26 <sup>i)</sup>	
2.82	11.25 <sup>j)</sup>	
2.80	11.22 <sup>k)</sup>	
2.80	11.10 <sup>l)</sup>	
3.00	0.07 <sup>m)</sup>	
2.03	1.36 <sup>n)</sup>	
2.78	0.35 <sup>o)</sup>	

a) Standard deviations range from  $\pm 0.002$  to 0.05.

b) All concentration units in  $mol\ dm^{-3}$ . c) Average first-order rate constants with respect to the disappearance of  $Fe(CN)_6^{3-}$  at 420 nm. d) Average  $k_{cat}(calcd)$  calculated from Eq. 16 (representative). e) Under an atmosphere of nitrogen gas;  $[Fe(CN)_6^{3-}]_0 = 1.0 \times 10^{-3}$ . f) For the disappearance of  $S_2O_3^{2-}$  at 217 nm;  $[Fe(CN)_6^{3-}]_0 = 1 \times 10^{-5}$ . g, h) Respectively at 0.42 and 0.52  $mol\ dm^{-3}$  of ionic strength. i, j, k, l) Respectively at 30, 40, 45, and  $60^\circ C$ . m, n, o) Respectively in the presence of  $1.0 \times 10^{-4}$   $mol\ dm^{-3}$  of added mannitol, acrylonitrile or  $Fe(CN)_6^{4-}$ .

or

$$k_{cat}(1 + K_{Os} K_2 [S_2O_3^{2-}]) = k_6 K_{Os} K_2 [Os(VIII)] [OH^-] [S_2O_3^{2-}]. \quad (16)$$

A plot of  $k_{cat}(1 + K_{Os} K_2 [S_2O_3^{2-}])$  vs.  $[S_2O_3^{2-}]$  should be a straight-line. At constant  $[Os(VIII)]$  and  $[OH^-]$ , employing the experimental value of  $K_{Os}$  and the computed value of  $K_2$ , the  $k_6$  value for this system at  $35^\circ C$  and  $\mu = 0.32\ mol\ dm^{-3}$  can be calculated from the least-squares slope of the above straight-line (neglecting the small value of the intercept) as  $(3.31 \pm 0.3) \times 10^{-2}\ dm^6\ mol^{-2}\ s^{-1}$ . The  $k_{cat}(calcd)$  values, calculated with the above values of  $k_6$ ,  $K_{Os}$ , and  $K_2$ , agree with those obtained experimentally lending credence to the proposed rate expression.

Inasmuch as the redox potentials<sup>24)</sup> for the couples  $S_2O_3^{2-}/S_4O_6^{2-}$  and  $Fe(CN)_6^{4-}/Fe(CN)_6^{3-}$ , are thermodynamically favourable for electron-transfer from thio-

sulfate to  $\text{Fe}(\text{CN})_6^{3-}$ , it is expected that the oxidation of thiosulfate to tetrathionate should proceed by a direct interaction between thiosulfate and hexacyanoferrate(III). In fact, in numerous oxidation studies of thiosulfate by metallic oxidants like complexes of  $\text{Cu}(\text{II})$ ,<sup>1)</sup>  $\text{Co}(\text{III})$ ,<sup>2)</sup>  $\text{Au}(\text{III})$ ,<sup>3)</sup>  $\text{Cr}(\text{VI})$ ,<sup>4)</sup> and  $\text{Fe}(\text{III})$ ,<sup>5)</sup> kinetic and other evidences suggest that intermediate metal-thiosulfato complexes (where the metal has lost one formal oxidation state and thiosulfate has gained one) are formed prior to the rate-determining electron-transfer step. Even though hexacyanoferrate(III) oxidations mostly involve outer-sphere electron change, in an analogous system<sup>25)</sup> involving hexacyanoferrate(III) and  $\text{SO}_3^{2-}$ , intermediate complexes of  $\text{Fe}(\text{CN})_5(\text{CNSO}_3)^{5-}$  and  $\text{Fe}(\text{CN})_5(\text{CNSO}_3)^{4-}$  have been evidenced in aqueous alkaline solution and definitely identified. Lancaster and Murray<sup>25)</sup> have suggested that many oxidations by transitional-metal complexes which are weak oxidants may proceed *via* intermediate complexes as described in the case of  $\text{Fe}(\text{CN})_6^{3-}$ - $\text{SO}_3^{2-}$  system. Legros<sup>26)</sup> has also reported that the hydrolysis of  $\text{Fe}(\text{CN})_5(\text{S}_2\text{O}_3)^{5-}$  in aqueous medium is accompanied by a high activation energy and positive activation entropy.

In the present system, however, no indication of any intermediate complex could be obtained from repeated and continuous scanning of the reaction solutions (from 250 nm to 650 nm). Also if the experiment is conducted in the presence of  $^{14}\text{CN}^-$ , there is no labelled cyano-ligand in the  $\text{Fe}(\text{CN})_6^{4-}$  product ensuring the absence of cyano exchange. Any direct interaction between hexacyanoferrate(III) and thiosulfate to form an intermediate complex necessitates a thiosulfato-ligand of very low Lewis-basicity to substitute or attach itself to, a cyano-ligand in a non-labile low-spin  $d^5$ -octahedral complex  $\text{Fe}(\text{CN})_6^{3-}$ , and this is inherently not allowed in all probability. A comparison of the divergent  $pK$  of  $\text{CN}^-$  and  $\text{SO}_3^{2-}$  with that of  $\text{S}_2\text{O}_3^{2-}$  (respectively 9.1, 9.1, and 1.9)<sup>15c)</sup> would show that even if any analogous complexes of  $[\text{Fe}(\text{CN})_5(\text{CNS}_2\text{O}_3)^{5-}]$  and  $[\text{Fe}(\text{CN})_5(\text{CNS}_2\text{O}_3)^{4-}]$  are thought of, they would not be stable enough in aqueous alkaline medium to be experimentally distinguishable.

However, in view of the expected higher redox potential of the couple  $\text{Os}(\text{VIII})/\text{Os}(\text{VI})$ , the  $d^0$ -configuration of  $\text{Os}(\text{VIII})$  and the decreased  $10Dq$  value of  $\text{Os}(\text{VIII})$  in the substitution of an octahedral complex, as compared to that in a substitution-inert  $\text{Fe}(\text{CN})_6^{3-}$ , the substitution of a hydroxo-ligand by a thiosulfato-ligand in *trans*-dihydroxotetraoxosmate(VIII) is possible. The intermediate complex thus formed, between  $\text{Os}(\text{VIII})$  and  $\text{S}_2\text{O}_3^{2-}$ , undergoes hydrolysis (in the direct oxidation reaction by  $\text{Os}(\text{VIII})$ ) with concomitant electron transfer, or is involved in an outer-sphere electron-transfer in the presence of alkaline hexacyanoferrate(III) in a termolecular rate-determining step.

Evidences for the presence of  $\text{S}_2\text{O}_3^-$ , thiosulfate(1-), have been well presented.<sup>5)</sup> In the present system radical-trapping agents retard the rate; polymerisation, however, is not detected. This may be because  $k(\text{S}_2\text{O}_3^- + \text{S}_2\text{O}_3^-) \gg k$  (induced polymerisation) so that

the induced change is too insignificant to be practically detectable. Moreover, absence of polymerisation does not necessarily mean absence of radical formation; in acidic medium, in the presence of dissolved oxygen, acrylonitrile does not polymerise even if the process is initiated by  $\gamma$ -radiolysis or by thermal decomposition of peroxodisulfate.

A reprisal of the data in Table 3 shows that there is a near-linear- $k_{\text{cat}}$  vs.  $[\text{S}_2\text{O}_3^{2-}]$ -relationship. To verify the validity of Eq. 16, experiments at higher  $[\text{S}_2\text{O}_3^{2-}]_0$  appear necessary; such an investigation is precluded as the  $[\text{S}_2\text{O}_3^{2-}]$ -dependence beyond  $[\text{S}_2\text{O}_3^{2-}]_0 = 24.6 \times 10^{-4} \text{ mol dm}^{-3}$  tends to be somewhat different from that observed in the concentration range employed suggesting that another reaction path<sup>27)</sup> probably becomes important at higher  $[\text{S}_2\text{O}_3^{2-}]_0$ .

The reactions are accompanied by an imperceptible temperature co-efficient in the range 30–60 °C as there is no appreciable change in the rate. This is probably due to the fact that the reaction has been studied at or very near the isokinetic temperature. We cannot offer at this stage any other reasonable explanation for this than that the large negative activation entropy created in the substitution step is probably counterbalanced by the more positive activation enthalpy in the electron-transfer step so that the net  $\Delta G^* \approx 0$ , thus causing no appreciable rate constant variation.<sup>23b)</sup>

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27) At higher  $[S_2O_3^{2-}]_0$ , there is probably a further interaction involving the product  $S_4O_6^{2-}$ , in addition to the involvement of one more  $S_2O_3^{2-}$  molecule; this should, we feel, provide the basis for further fruitful study.